

BGP non-convergence

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Introduction

- BGP has no guaranteed convergence
- Other routing protocols, they try to solve the shortest path problem
- What problem tries to solve BGP?
- The stable path problem formulation

Modeling BGP route selection (I)

- Simplifying assumptions
 - Ignore IBGP related issues
 - Ignore MED attribute
 - Assume at most one link between two ASes
 - Ignore Route aggregation
- Information contained in UPDATE records
 - Nlri
 - next-hop
 - as_path
 - local_pref
 - c_set
- Ranking: for the same nlri

$$rank_tuple(r) = \left\langle r.local_pref, \frac{1}{r.as_path}, \frac{1}{r.next_hop} \right\rangle$$

Modeling BGP route selection (II)

- Route transformation $T(r)$: operates by deleting, inserting or modifying attributes values
- If u and w autonomous systems, the a record moves from u to w suffers the following transformations:
 - $r_1 = \text{export}(u \leftarrow w, r)$ export policies defined by w
 - $r_2 = \text{PVT}(u \leftarrow w, r_1)$ Path Vector Trans
 - add w to AS path, sets next hop, filters loops
 - $r_3 = \text{import}(u \leftarrow w, r_2)$ import policies defined by u
- Peering transformation
 - $pt(u \leftarrow w, r) = \text{import}(u \leftarrow w, \text{PVT}(u \leftarrow w, \text{export}(u \leftarrow w, r)))$

Modeling BGP route selection (III)

- AS u_0 is the origin of a destination d sending record r_0
- AS U_k and $P = u_k u_{k-1} \dots u_0$ a path, then $r(P)$ is the route record received at u_k from u_0
 - $r(P) = \text{pt}(u_k \leftarrow u_{k-1}, \text{pt}(u_{k-1} \leftarrow u_{k-2}, \dots, \text{pt}(u_1 \leftarrow u_0, r_0) \dots))$
 - P is permitted at u_k if $r(P)$ is non empty
- Ranking function

$$\lambda^{u_k}(P) = \text{lexical_rank}(\text{rank_tuple}(r(P)))$$

Stable Path Problem (SPP) (I)

- $G=(V,E)$, simple undirected graph
 - $V=\{0,1,\dots,n\}$ nodes
 - E , set of edges
- Node 0 (origin) special cause is the destination
- $\text{peers}(u)$
- Path: $P = (v_k, v_{k-1}, \dots, v_0)$ seq of nodes
- For each v of V , P^v is set of permitted paths
- P is the union of all P^v
- For each v , ranking function $\lambda^v(P)$ where P is in P^v
 - $\lambda^v(P_1) > \lambda^v(P_2) \Rightarrow P_1$ is preferred
 - $\Lambda = \{\lambda^v / v \text{ belongs to } V - \{0\}\}$

Stable Path Problem (SPP) (II)

- Instance of the SPP $S=(G,P,\Lambda)$ (graph, set of permitted paths and ranking functions) and:
 - $P^0=\{\{0\}\}$ and for all v except 0
 - Empty path is permitted
 - Empty path is always ranked last
 - Strictness: If $P_1 \neq P_2$ and $\lambda^v(P_1) > \lambda^v(P_2) \Rightarrow$ they have the same next hop
 - Simplicity: all paths in P have no repeated nodes

Stable Path Problem (SPP) (III)

- Instance of the SPP $S=(G,P,\Lambda)$
- Path assignment function π maps a node u to a path $\pi(u)$ from P^u
 - $\pi(u)$ empty means u has no path to the origin
- Path choices(π, u)

$$choices(\pi, u) = \begin{cases} \{(uv)\pi(v)/\{u,v\} \in E\} \cap P^u, & u \neq 0 \\ \{(0)\}, & o.w. \end{cases}$$

- W subset of P^u with different next hop

$$best(W, u) = P \in W, \max \lambda^u(P)$$

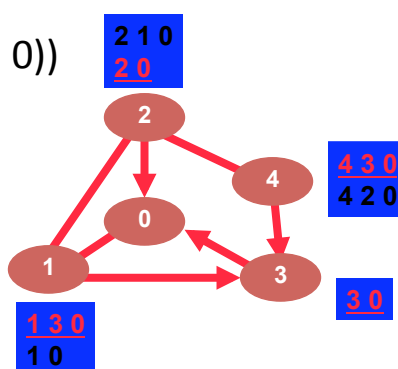
Stable Path Problem (SPP) (IV)

- A path assignment π is stable at a node u if

$$\pi(u) = \text{best}(\text{choices}(\pi, u), u)$$
- A SPP $S = (G, P, \Lambda)$ is solvable if there is a stable path assignment for all u of S

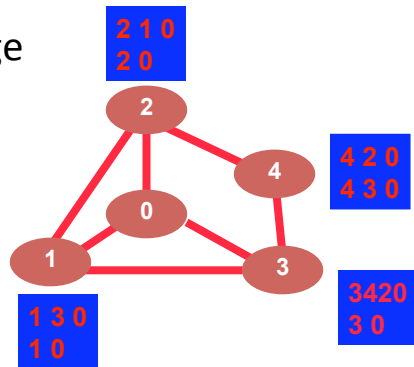
Example 1: good gadget

- Only one solution
- $((1\ 3\ 0), (2\ 0), (3\ 0), (4\ 3\ 0))$
- Note that not only shortest paths are preferred

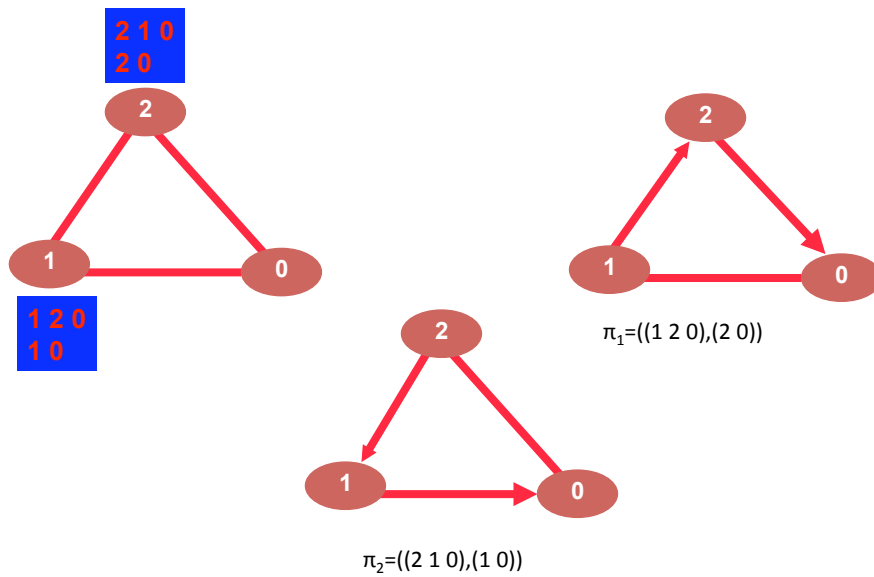


Example 2: bad gadget

- No solution
- Protocol always diverge



Example 3: Disagree



Simple Path Vector Protocol (SPVP)

- Abstract version of BGP
- Always diverges when the SPP has no solution
- Assume reliable FIFO queue for messages
- Messages exchanged are simply paths
- When node u adopts one path P from P^u , it informs all its peers by sending them P
- Data structures in u
 - $\text{rib}(u)$ contains current path to the origin
 - $\text{rib-in}(u \leq w)$ for each w , stores the most recent path
- $\text{choices}(u) = \{(u \ w)P \text{ of } P^u \mid P = \text{rib-in}(u \leq w)\}$
- Best possible path: $\text{best}(u) = \text{best}(\text{choices}(u), u)$

SPVP algorithm

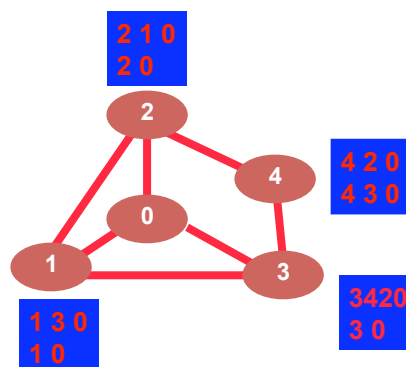
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process svpv(u)
begin
  receive P from w
  begin
    rib-in(u<=w):=P
    if rib(u) ≠ best(u) then
      begin
        rib(u):=best(u)
        for each v of peers(u) do
          begin
            send rib(u) to v
          end
        end
      end
    end
  end
end

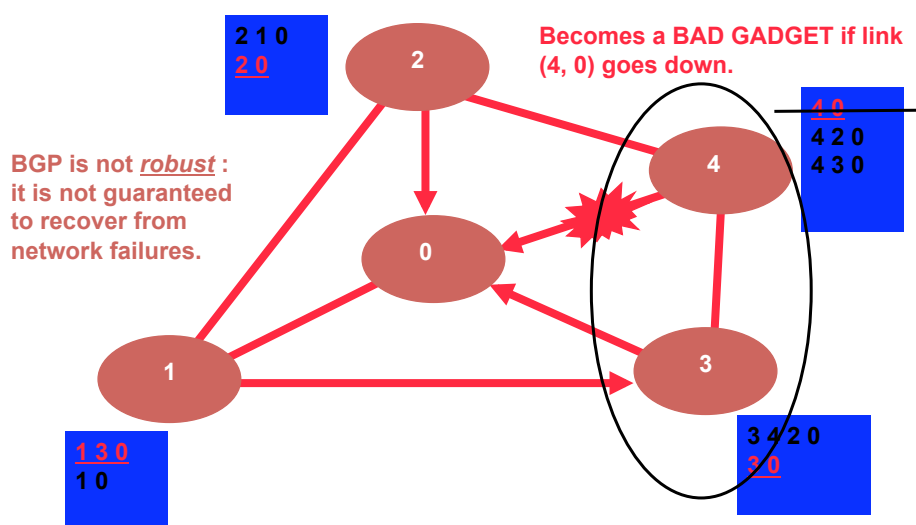
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SPVP and the bad gadget

step	π
0	(1 0) (2 0) (3 4 2 0) (4 2 0)
1	(1 0) (<u>2 1 0</u>) (3 4 2 0) (4 2 0)
2	(1 0) (2 1 0) (3 4 2 0) <u>ε</u>
3	(1 0) (2 1 0) (<u>3 0</u>) ε
4	(1 0) (2 1 0) (3 0) (<u>4 3 0</u>)
5	(<u>1 3 0</u>) (2 1 0) (3 0) (4 3 0)
6	(1 3 0) (<u>2 0</u>) (3 0) (4 3 0)
7	(1 3 0) (2 0) (3 0) (<u>4 2 0</u>)
8	(1 3 0) (2 0) (<u>3 4 2 0</u>) (4 2 0)
9	(<u>1 0</u>) (2 0) (3 4 2 0) (4 2 0)



System may become unstable after a failure



Stability and safety

- Network states are the collection of values of $\text{rib}(u)$, $\text{rib-in}(u \leq v)$ and state of communication links
- A network state is stable if communications links are empty
- Path assignment of a stable network state is a stable path assignment
- A stable path problem is safe if the SPVP always converge

Dispute wheels (I)

- Determining if a stable path assignment exists is an NP hard problem
- Dispute wheels are an heuristic to find a stable path assignment
- Suppose V' contained in V such that 0 is in V'
- Partial path assignment π for V' is a path assignment such as
 - For all u of V' , every node in $\pi(u)$ is in V'
- Heuristic procedure to construct seq $V_0 \subset V_1 \subset \dots \subset V_n$ along with $\pi_0, \pi_1, \dots, \pi_n$ partial assignments for V_i
- Then for each π_i we construct π'_i such as
 - $\pi'_i(u) = \pi_i(u)$ for u of V_i
 - $\pi'_i(u)$ is empty for other u

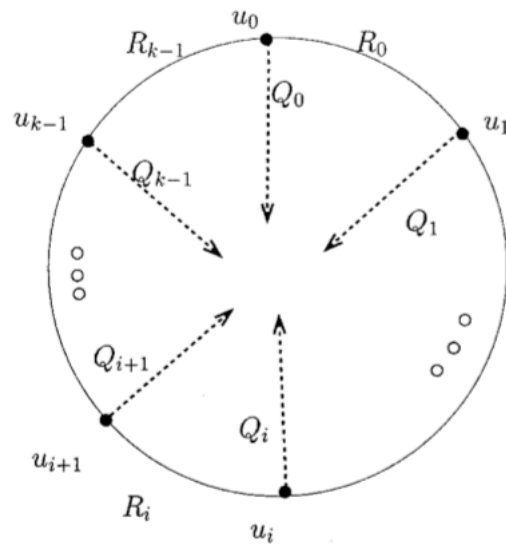
Dispute wheels (II)

- If u belongs to $V-V_i$ and P belong to P^u , then P is consistent with π_i if
 - $P=P_1(u_1 u_2)P_2$ where P_1 is a path in $V-V_i$ and u_2 belong to V_i and $P_2=\pi(u_2)$ and $\{u_1 u_2\}$ belongs to E
 - P is called direct path to V_i if P_2 is empty
- Let D_i be the set of nodes u of $V-V_i$ that have a direct path to V_i
- Let H_i the set of nodes of D_i that highest ranked path consistent with π_i is a direct path
 - This path is called B_i^u
- Let $V_{i+1} = V_i + H_i$
- Define partial assignment $\pi_{i+1}(u) = \begin{cases} B_i^u, u \in H_i \\ \pi_i(u), u \in V_i \end{cases}$
- Continue till either $V_k=V$ or $V_k \neq V$ and $H_k=0$

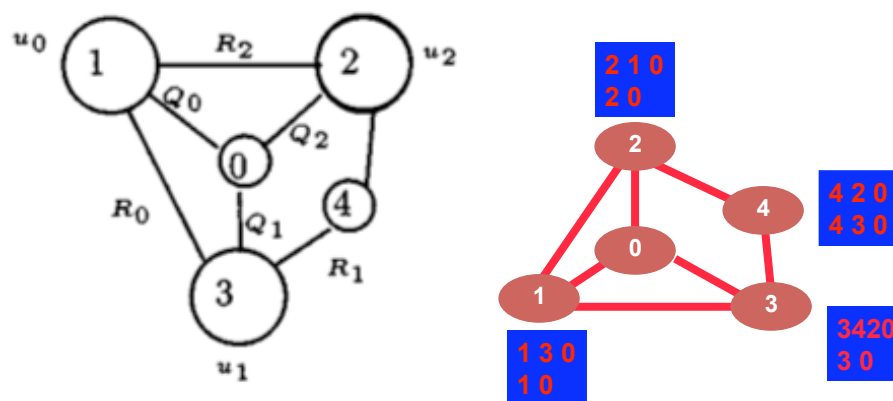
Dispute wheels (III)

- If we are in the second case, we have a circular set of conflicting rankings between nodes, called a dispute wheel
- Dispute wheel $\Pi = (\vec{U}, \vec{Q}, \vec{R})$ of size k
 - Seq of node $\vec{U} = u_0, u_1, \dots, u_{k-1}$
 - Seq of non empty paths $\vec{Q} = Q_1, Q_2, \dots, Q_{k-1}$ $\vec{R} = R_1, R_2, \dots, R_{k-1}$
 - Such that for for each $0 \leq i \leq k-1$
 1. R_i is a path from u_i to u_{i+1}
 2. Q_i belongs to P^{u_i}
 3. $R_i Q_{i+1}$ belongs to P^{u_i}
 4. $\lambda^{u_i}(Q_i) \leq \lambda^{u_i}(R_i Q_{i+1})$

Dispute wheel (IV)



Dispute wheel for bad gadget



Properties of Dispute wheels

- No dispute wheel implies solvability
- No dispute wheel implies a unique solution
- No dispute wheel implies safety

Can we guarantee that BGO will not diverge?

- Operational practices
 - See next section
- Static analysis
 - Routing policy registry
 - Check for convergence
 - NP hard problem
 - ASes don't want to show policy information
- Dynamic solution?

Reference

- IEEE/ACM TRANSACTIONS ON NETWORKING, VOL. 10, NO. 2, APRIL 2002 The Stable Paths Problem and Interdomain Routing, Timothy G. Griffin, F. Bruce Shepherd, and Gordon Wilfong

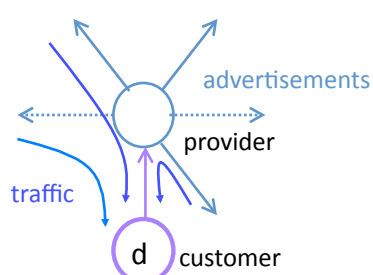
Relationships between ASes

- Peering
- Transit

Transit relationship

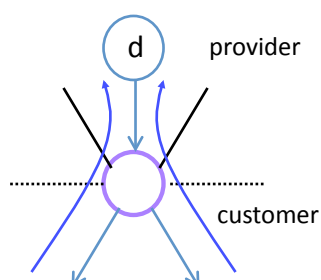
- ◆ Customer pays provider for access to the Internet
 - Provider exports its customer's routes to everybody
 - Customer exports provider's routes only to downstream customers

Traffic **to** the customer



slide form Rexford

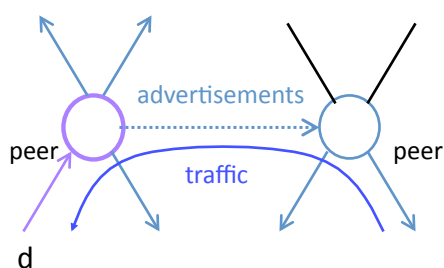
Traffic **from** the customer



Peer relationship

- ◆ Peers exchange traffic between their customers
 - AS exports *only* customer routes to a peer
 - AS exports a peer's routes *only* to its customers

Traffic to/from the peer and its customers

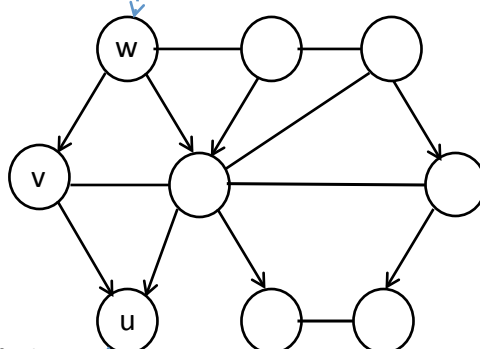


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Resulting hierarchy

◆ Provider-customer graph is a directed, acyclic graph

- If u is a customer of v and v is a customer of w
- ... then w is *not* a customer of u



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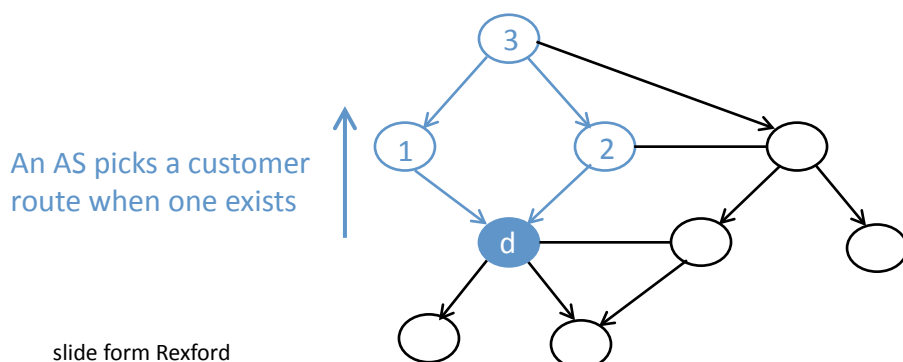
Proposed route selection

- Classify routes based on next-hop AS
 - Customer routes, peer routes, and provider routes
- Rank routes based on classification
 - Prefer *customer* routes over peer and provider routes
- Allow *any* ranking of routes within a class
 - E.g., can rank one customer route higher than another
 - Gives network operators the flexibility they need
- Consistent with traffic engineering practices
 - Customers pay for service, and providers are paid
 - Peer relationship contingent on balanced traffic load

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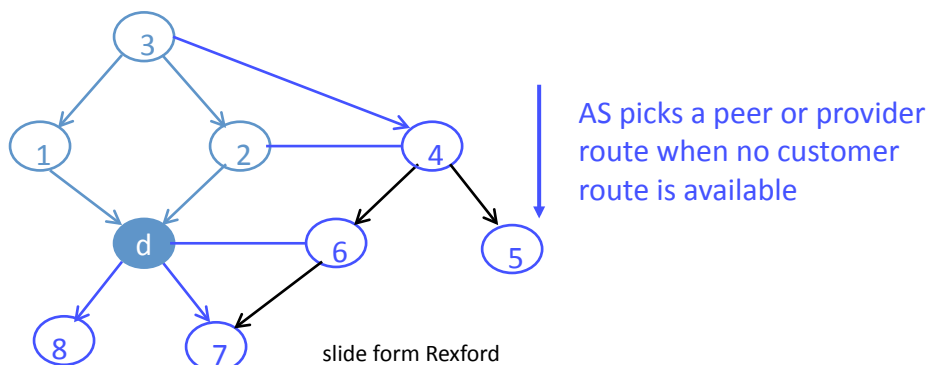
Proof, Phase 1: Selecting Customer Routes

- Activate ASes in customer-provider order
 - AS picks a customer route if one exists
 - Decision of one AS cannot cause an earlier AS to change its mind



Proof, Phase 2: Selecting Peer and Provider Routes

- Activate rest of ASes in provider-customer order
 - Decision of one phase-2 AS cannot cause an earlier phase-2 AS to change its mind
 - Decision of phase-2 AS cannot affect a phase 1 AS



Reference

- L. Gao, J. Rexford, Stable Internet routing without global coordination
- <http://www.cs.princeton.edu/~jrex/teaching/spring2005/reading/gao01.pdf>

Assignment

- Theorem 5.1 & proof
- Theorem 5.2 & proof
- Theorem 5.3 & proof